FINITE ELEMENT RECONSTRUCTION OF DECOMPRESSIVE CRANIECTOMY

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Abstract

Traumatic brain injuries (TBIs) have a devastating global epidemiological importance since they contribute to the mortality and morbidity in the society with a considerably large extent. After TBI the injured brain tissue tends to swell leading to the increment of the intracranial pressure (ICP) which can cause serious neurological damage and death. Therefore, a main goal of the neurosurgical procedure is the reduction of ICP which is possible via decompressive craniectomy (DC). However, its optimal execution regarding the size and the location of the skull opening is controversial. In this paper the reconstruction of DC is performed by finite element (FE) simulations. The applied modelling strategy is presented and patient-specific FE models are constructed with different levels of anatomic details which can predict the post-operative response of the brain tissue for a given pre-operative state. These models are validated by reconstructing real life DC case, where the predicted displacements and ICP are compared to their observed value measured by neurosurgeons. Results confirm the applicability of the above described modelling procedure, implying that such models can be used to optimize DC in the future based on the biomechanical response of the highly deformable brain tissue.

Keywords: traumatic brain injuries, decompressive craniectomy, finite element simulations, intracranial pressure, Computer-Assisted Neurosurgery

Introduction

Traumatic brain injuries (TBIs) have a devastating global epidemiological importance since they contribute to the mortality and morbidity in the society with a considerably large extent.¹ One of the most important complications of TBIs is brain edema consisting of an abnormal fluid accumulation within the injured parenchyma and swelling of the brain. Brain swelling can lead to secondary injury by uncontrolled increment of intracranial pressure (ICP) which can cause serious neurological damage and death.²⁻⁵ Accordingly, edema and its complications account for approximately 50% of death in patients with TBI,⁶ therefore an important goal of the treatment is the reduction of ICP. Reduction of ICP can be achieved by decompressive craniectomy (DC) which can be used sometimes as a last-tier (i.e. an ultimate life-saving) surgical procedure.⁷⁻¹⁰ In this operation a piece of skull is removed and the underlying dura mater is opened (Figure 1) in order to allow the brain to expand outside the skull bone resulting in a bulging deformation and the mitigation of ICP.^{11,12}



Figure 1. Main steps of decompressive craniectomy. *a)* skin; *b)* skull and *c)* dura incision indicated by the dotted lines¹³

Despite the ICP reduction, axonal fibres are subjected to extreme stretching which is thought to contribute to an unfavourable neurological outcome for patients treated with DC.^{14,15} Effective treatment of brain edema is challenging since the optimal execution of DC regarding the size and the location of skull opening is controversial¹³ and the recommended treatment is based on clinical practice and personal experience.^{16,17} Therefore, there is a need for developing new methods which can predict the biomechanical response of the swollen brain tissue. Accordingly, a long-term research goal can be formulated as performing a comprehensive optimization of DC based on the biomechanical response of the highly deformable brain tissue.¹⁸

Despite the enormous complexity of the brain, many aspects of its response can be described in purely mechanical terms, such as displacements, strains and stresses.¹⁹ The latest trend in biomechanical research of brain injuries is performing finite element (FE) simulations²⁰⁻²² in order to determine the mechanical response of the human brain. There are several applications of biomechanical models in Computer-Assisted Neurosurgery¹⁹ related to hydrocephalus²³⁻²⁵ and image-guided surgery in case of tumour resection,^{26,27} however, there is a lack of biomechanical research dealing with DC²⁸ since only a relatively few studies have been performed by now. Gao and Ang¹⁸ presented the first 3D head model which was used to simulate ICP distribution and tissue deformation following DC. A poroelastic material model was applied for the brain tissue whose parameters were taken based on previous research, however they did not provide experimental validation of their model. Nevertheless, based on qualitative comparison of the calculated and observed brain deformations, it was concluded that FE models can be able to simulate DC. Furthermore, it was observed that the size of the craniectomy influences the reduction of ICP and the deformations of the tissue, thus it was hypothesized that an optimum should exist regarding the size of the skull opening. Moreover, the maximum stress regions were found near the craniectomy, which was confirmed by Holst et. al²⁹ via determining strains and water content in brain tissue by nonlinear medical image registration (MIR).

Later,³⁰ finite element models were developed with poroelastic tissue behaviour to reconstruct DC cases, and model validation was performed based on observed deformations of the brain tissue. Fletcher et. al³¹ developed a simplistic FE model in order to reconstruct physical experiments performed on a surrogate model. Several material models were investigated for modelling the mechanical response of the brain tissue and it was found that the time-dependent material behaviour of the brain was not critical to the conditions at the early stages of loading when the peak strain occurred. Experiments³² have shown that the mechanical behaviour of the brain tissue is similar to the behaviour of filled elastomers, thus later finite element head model was developed³³ using Ogden's second order isotropic hyperelastic material model³⁴⁻³⁶ for modelling the behaviour of the parenchyma. This model was not a patient-specific model since its geometric features were taken from the Collins Brain Atlas.³⁷ It was applied to determine maximum bulge displacement and volume exceeding a critical shear strain for different craniectomy types (unilateral, bilateral, bifrontal, etc).

As a summary of literature review, it is mentioned that during the optimization of DC the ICP and the strain of the parenchyma can be considered as objective functions which should be minimized. Previously mentioned models^{18,30,33} were able to predict the deformations of the brain tissue, however ICP was not validated and in certain cases its value corresponding to the pre-operative (pre-op) state was used as natural boundary conditions at the boundaries of the parenchyma.¹⁸ According to previous efforts,^{18,33} the optimization of DC would include several simulations of DC which start from a given pre-op state and their execution is performed with different craniectomy sizes and locations, while resulting ICP and strains are monitored. This procedure would require the development of FE models which reliably predict not just strains but ICP of the parenchyma as well.

This paper presents a modelling strategy which can be used as a tool for the optimization of DC in the future. The development of 3D patient-specific head models are discussed in detail. By following these steps, two FE models are developed with different levels of anatomic details. These models are validated by reconstructing a real-life DC case where the predicted and observed ICP and deformations are compared.

Methods

According to previous research,²⁹ our modelling procedure starts from an initial reference state, where the geometry represents an approximated patient-specific healthy state. Since medical images of patients in the healthy state are not available in general, the healthy intracranial state is approximated by nonlinear MIR²⁹ using Computer Tomography (CT) images of healthy volunteers. However, it should be taken into account that the relative volume of ventricles (RVV) (i.e. the volume of lateral ventricles divided by the intracranial volume) has a relatively large variability among humans and ventricle volumes are age-dependent.³⁸ Therefore, in order to obtain an approximated average healthy state, three groups of volunteers were identified age-dependently (Group I for volunteers aged between 18-39 years, Group II for volunteers between 40-69 and Group III for volunteers elder than 70 years), and CT scans of 15 volunteers were used for each group respectively. The RVV was calculated for each volunteer by segmentation of CT images performed in 3D Slicer environment.³⁹ Afterwards, the obtained RVVs were considered as a statistical sample for each group, and one volunteer having the median RVV was chosen for each group respectively. With the application of this statistical procedure, working with a healthy volunteer having extremely small or extremely large ventricles was avoided.

The patient-specific healthy state is approximated by nonlinear MIR using B-splines⁴⁰ performed in 3D Slicer, where CT images of the chosen healthy volunteer (*Figure 2.a*) are morphed to the patient's CT images at the pre-op (i.e. injured) state (*Figure 2.b*) based on the patient's cranial shape.²⁹ The result of this transformation is a sequence of CT images where the cranial shape approximately agrees with the patient's cranial shape, but the shape of the intracranial anatomic parts represent an average healthy condition (*Figure 2.c*).



Figure 2. Estimation of patient-specific healthy state by nonlinear medical image registration.a) CT scan of a healthy volunteer; b) CT scan of the patient at the pre-op state;c) CT scan of the approximated healthy condition

Segmentation of different parts of the human head can be performed on these CT images in 3D Slicer environment. In order to investigate the sensitivity of results due to the applied modelling level, two different models are created which represent different anatomic details.

The simplistic model (Model A) includes the parenchyma, the outer cerebrospinal fluid (CSF) space, the skull bone and dura mater (considered as one merged volume having a several magnitudes larger stiffness than the parenchyma), while the more complex model (Model B) contains the lateral ventricles and the falx cerebri as well. Due to convergence issues which were a barrier of previous research,³³

ventricles and the outer CSF space is not modelled by solid parts, but these are represented by cavities in the geometry. The supporting effect of CSF on the surface of the parenchyma is taken into account by a pressure load with 5 Hgmm intensity (approximating an initial healthy state) and an elastic spring support in order to model the increased ICP at the boundaries due to swelling. After the segmentation, surface models are obtained for each anatomic part which contain sharp edges and gaps, therefore their smoothing and correction are performed in Meshlab⁴¹ by VCG reconstruction.⁴² Afterwards, the smoothed surface models can be converted to 3D CAD geometry (Figure 3.a-b) which is performed in Ansys



Figure 3. Geometry and mesh of the patient-specific FE model.a) Geometry of the brain and the opened skull; b) Geometry of lateral ventricles;c) FE mesh of the brain tissue and the falx cerebri

SpaceClaim⁴³ environment. The obtained geometry can be imported to Ansys Workbench⁴⁴ environment where the finite element model is developed (*Figure 3.c*).

In order to separate FE mesh generation from the unimportant geometric features, a virtual topology⁴⁴ is constructed by generating virtual cells. Afterwards, a patch independent finite element mesh⁴⁴ is constructed consisting of tetrahedral finite elements for solid volumes and shell elements for the falx (*Figure 3.c*). In accordance with previous research,³³ parenchyma is considered as an isotropic, hyperelastic material modelled by a second-order Ogden material model³⁴⁻³⁶ whose strain energy function U is shown in Equation 1:

$$U = \sum_{i=1}^{2} \frac{2\mu_{i}}{\alpha_{i}^{2}} \Big(\lambda_{1}^{\alpha_{i}} + \lambda_{2}^{\alpha_{i}} + \lambda_{3}^{\alpha_{i}} - 3 \Big), \qquad (1)$$

where parameters and describe the shear modulus, parameters and characterize the strain hardening effect (*Table 1*) and are the deviatoric principal stretches. The mechanical behaviour of the skull and the falx is simulated by a linear elastic material model used in previous model⁴⁵ whose Young's modulus and Poisson's ratio are listed in *Table 1*.

According to previous research,²⁹ modelling of DC consists of two stages. In the first stage the brain swelling is modelled, i.e. an injured preop state is obtained from the initial healthy state. Brain swelling is obtained by artificial thermal expansion³³ of the parenchyma leading to the increased ICP in the pre-op state. The distribution of the thermal loading depends on the actual injury type and can be estimated by the Hounsfield-unit⁴⁶⁻⁴⁸ obtained from CT images.

In the current case, edema was modelled by a uniformly distributed thermal loading of the parenchyma supplemented by an additional local thermal expansion which causes an increased ICP near the focal contusion of the tissue. The magnitude of the thermal loading is determined by a calibration procedure, where the applied temperature is calculated by the false position method⁴⁹ based on the equality of the observed and predicted ICP of the parenchyma at the pre-op state near the lateral ventricles. Finite element nodes of the skull and the outer edges of the falx are rigidly supported against translational displacements, while the surface of the parenchyma is elastically supported by spring elements representing the supporting effect of CSF. Furthermore, a frictionless contact is established between the skull and the parenchyma, and the brain and the falx.

In the second stage DC is performed, thus the post-op state is obtained from the preop state by removing a portion of the skull and dura via prescribed displacements. In this step the supporting effect of CSF near the skull opening is neglected and the bulging deformation of parenchyma is obtained.

Anatomic part	Material model	Material parameters	
Skull	Linear elastic	E = 15000 MPa	v = 0,22
Dura mater and falx cerebri	Linear elastic	E = 31,5 MPa	v = 0,45
Brain tissue	Hyperelastic	$\mu_1 = 1,044 \text{ kPa}$	$\alpha_1 = 4,309$
		$\mu_2 = 1,183 \text{ kPa}$	$\alpha_2 = 7,736$

Table 1. Applied material models and parameters



Figure 4. Observed and simulated results (obtained by Model A) at the pre-op state. *a)* CT scan; *b)* simulated displacements; *c)* simulated ICP



Figure 5. Observed (a) and simulated (b) bulging deformation of the brain tissue



Figure 6. Observed and simulated results (obtained by Model A) at the post-op state. *a*) CT scan; *b*) simulated displacements; *c*) simulated ICP



Figure 7. Von Mises stresses of the parenchyma [kPa]. a) stress peaks near the perimeter of craniectomy; b) stresses in an axial section



a) displacements; b) ICP; c) von Mises stresses

Results

In this section, results of the model validation are shown corresponding to the reconstruction of a real-life DC case. Simulated deformations and ICP of the parenchyma obtained by Model A at the pre-op state is shown in *Figure 4.b-c.*

Afterwards, the simulation of skull removal was performed and a bulging deformation was obtained (*Figure 5.b*) which is similar to the observed deformations (which was obtained by the segmentation) of the brain tissue (*Figure 5.a*). Results at the post-op state in terms of displacements and ICP (obtained by Model A) are shown in Figure 6.b-c.

Von Mises stresses of the parenchyma at the postop state obtained by Model A is shown in *Figure 7*.

Results obtained by Model B corresponding to the post-op state are shown in *Figure 8*.

Beside the qualitative comparison, a quantitative analysis was also performed of the predicted and observed results (Table 2). The simulated ICP values show the average ICP obtained in finite elements which belong to a sphere with 5 cm diameter around the ventricles.

	Measured	Predicted by Model A	Predicted by Model B
Max. displacement [mm]	≈17	13,03	11,89
Pre-op ICP [Hgmm]	18	18,10	18,07
Post-op ICP [Hgmm]	12	12,19	14,52

Table 2. Quantitative comparison of observed and predicted results

Discussion

In this paper a finite element modelling strategy of decompressive craniectomy has been detailed and corresponding patient-specific models were constructed with different anatomic details. Model validation has been performed by reconstructing a real-life case where qualitative and quantitative comparison of simulated and observed displacements and ICP were made. Resulting from the calibration procedure, ICP near the lateral ventricles at the pre-op state (Figure 4.c) fits well to its measured value (Table 2). A qualitative analysis of bulging displacements based on results of FE simulations (Figure 5, Figure 6.a-b, Figure 8.a) showed that the predicted displacements of the parenchyma approximates well the observed deformations in case of both models.

The quantitative comparison showed that the difference in terms of maximal displacements between predicted and observed results is about 4-6 mm (*Table 2*), which is considered here as an acceptable agreement. According

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to our results corresponding to the post-op state (Figure 6.c; Figure 8.b, Table 2) the simulated ICP values obtained by both models fit relatively well to the measurements performed at the clinic. Results of the von Mises stresses obtained by Model A (Figure 7.a) confirm that large stresses and strains occur near the perimeter of the craniectomy which could be responsible of poor neurological outcome. However, stress and strain peaks near the lateral ventricles whose existence was observed in previous study²⁹ could only be predicted by Model B (Figure 7.b, Figure 8.c), therefore it is concluded that the optimization in the future must be performed on models where lateral ventricles are included. Based on results obtained by Model B (Figure 8, Table 2), the currently applied modelling strategy can be an adequate tool for modelling DC. Following this modelling procedure, validated patient-specific FE models can be applied to optimize decompressive craniectomy in the future, by performing virtual experiments with different craniectomy size and locations while ICP and strains or stresses of the parenchyma are monitored.

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